Evaluation of the Cell Broadband Engine running Continuous Estimation of Distribution Algorithms

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Abstract—Current consumer-grade computers and game devices incorporate very powerful processors that can be used to accelerate many classes of scientific codes. However, programming multi-core chips, hybrid multi-processors or graphical processing units is not an easy task for those programmers that deal mainly with sequential codes. In this paper, we explore the ability of the Cell Broadband Engine to run a particular Estimation of Distribution Algorithm (Univariate Marginal Distribution Algorithm for the Continuous domain). From an initial sequential version, we develop a multi-threaded one that is afterwards reworked to run on a Cell. Both versions of the code show significant improvements in performance, compared to the sequential version. We analyze the results obtained and provide some clues about the performance/cost characteristics of the tested platforms.

Keywords—Cell Broadband Engine, Estimation of Distribution Algorithms in Continuous Domains, Parallel programming

I. INTRODUCTION

The recent popularization of consumer hardware with parallel capabilities, such as multi-core processors (including the Cell Broadband Engine) and GPUs, that we can find in personal computers and game consoles, brings out the potential of enormous computing power for a budget. However, exploiting this potential is not easy: programs have to be reworked in order to take advantage of these parallel, sometimes hybrid, processors. They require complex programming methods that are not easy for the casual programmer. Parallelism, a challenge by itself, is not the only issue. Unfamiliar memory models, limited instruction sets, explicit communications, etc. combine to make really hard the effective exploitation of theoretically powerful machines.

The availability of powerful computers (not necessarily parallel) with large amounts of memory has encouraged the design and implementation of non-trivial algorithms to solve different kinds of complex optimization problems. Some of these problems can be solved via an exhaustive search over the solution space, but in most cases this brute force approach is unaffordable. In these situations, heuristic methods (deterministic or non deterministic) are often used, which search inside the space of promising solutions. Some heuristic approaches are specifically designed to find good solutions for a particular problem, but others are presented as a general framework adaptable to many different situations. Among this second group (general designs), there is a family of algorithms that has been widely used in the last decades: Evolutionary Algorithms (EAs). This family comprises, as main paradigms, Genetic Algorithms (GAs) [1], [2], Evolution Strategies [3], Evolutionary Programming [4] and Genetic Programming [5]. Even though processing speeds grow fast, the requirements of this class of algorithms do even faster. No matter the computing power available, we can always find a harder problem that cannot run in our machines, or can do so but takes too long to run.

Therefore, we have the problem (the execution of complex optimization algorithms) and the platform (consumer-grade parallel hardware). We need to port the application to the target hardware, in order to efficiently exploit the latter, to accelerate program execution and/or obtain better solutions.

In this paper, we extend the work presented in [6], in which we tested the suitability of the Cell as a computing platform for one algorithm of the family of Estimation of Distribution Algorithms. In particular, we studied the Univariate Marginal Distribution Algorithm (UMDA), applied to solving the OneMax function, a well-known toy problem. Due to the characteristics of UMDA (discrete variables and simple probabilistic model) and the problem to solve, we observed a discouraging poor performance in terms of execution time and scalability, compared to that provided by a commodity multi-core personal computer. The main reason for this disappointing behavior has to be found in the computation/communication ratio of this particular program. As the vector units of the Cell have only a small local memory, the time needed to move data from/to the main memory dominated the overall execution time, thus impeding the full exploitation of the Cell’s power.

As the family of EDAs comprises algorithms in both discrete and continuous domains, we decided to extend our previous work by testing an algorithm similar to UMDA, but for continuous domains. It is called Univariate Marginal Distribution for the Continuous domain (UMDAc). The main purpose is to evaluate the performance of the Cell platform when working with floating-point numbers.

We followed the same methodology used to parallelize UMDA. Starting from an initial sequential version, the algorithm was ported to a parallelized ver-
The final results show that our parallel and vectorization techniques were applied in a second step. The parallel version was, afterwards, reworked to run on a multi-core, hybrid system (the Cell Broadband Engine). To further accelerate the programs, vectorization techniques were applied in a second step. The rest of the paper is organized as follows. Section II discusses the architecture of the Cell Broadband Engine, with special emphasis on those characteristics visible to the programmer. Section III summarizes the main characteristics of Evolutionary Algorithms and, in particular, the family of Estimation of Distribution Algorithms in the continuous domain and the problem to be solved with our implementation. Section IV explains the process of porting the algorithm and the vectorization process in the two platforms. Section VI shows the experiments made in order to compare both implementations.

II. CELL BROADBAND ENGINE

The Cell is a microprocessor system that integrates, into a single chip, a Power-based processor (Power Processing Element, PPE), eight vector co-processors (Synergistic Processing Elements, SPEs), a memory interface, input/output interfaces and a high-speed ring that acts as the interconnection fabric for the remaining elements [7] (see Figure 1, extracted from [8]). A programmer that wants to take full advantage of a Cell has to deal with two different instruction sets: one for the PPE and another one for the SPEs. This usually means using two compilers, and dealing with different strategies to optimize code running in different processors. To mention just an example, the PPE can deal with vector operations to accelerate parts of the program, but the SPEs must work with vectors – its efficiency with scalars is not brilliant.

Another peculiarity of the Cell is its memory organization. From a programmer’s point of view, the PPE has full, direct access to the system’s main memory. However, the SPEs have direct access only to a very limited sized (256 KB) local store. All the data processed by an SPE has to be previously transferred to its local store, and the resulting data, if required by the PPE or another SPE, has to be explicitly transferred too. To that purpose, each SPE has a companion Memory Flow Controller (MFC) that can take care of this transfer. A good programmer can manage to make an SPE and its MFC work at the same time, processing pieces of data while transferring new ones. A careless programmer may try to simultaneously move too much data through the interconnection fabric, which would become a bottleneck because of limited capacity.

Challenges for the programmer are, therefore, manifold: different instruction sets; real necessity of working with vector instructions; limited memory size; explicit transfer of data between different memory blocks, etc. Adaptation of an application to this architecture is not trivial: a few applications may have a natural mapping, but most require exhaustive reworking. A common model for organizing Cell applications, but by no means the only one, is to use the PPE as a main processor running most of the application’s logic, using the SPEs as acceleration co-processors [9]. The most compute-intensive sections of the original PPE-only code are identified, and reworked to make them run in parallel in the available SPEs. As just mentioned, this is a complex task that requires careful organization of data structures, data movement, synchronization, vectorization, etc.

Regarding hardware platforms, IBM sells Cell-based systems for use as general-purpose systems, but the most popular, consumer-available platform to get acquaintance with this processor is Sony’s PlayStation 3 game console. The PS3 can be easily converted in a GNU/Linux “computer” with all the necessary toolkits to develop and run Cell applications, by means of any of the several available Linux distributions. The main limitation of this platform is that only six SPEs are available: Sony guarantees just seven working SPEs (to increase manufacture yield), and one is always reserved for the operating system. In this work we use a PS3 running Fixstars’ Yellow Dog Linux [10].

III. EVOLUTIONARY ALGORITHMS

The main characteristic of Evolutionary Algorithms is that they use techniques inspired by the natural evolution of the species. In nature, species change across time; individuals evolve, adapting to the characteristics of the environment. This evolution leads to individuals with better characteristics. This idea can be translated to the world of computation, using similar concepts:

- **Individual:** Represents a possible solution for the problem to be solved. Each individual has a set of characteristics (genes) and a fitness value (based on its genes) that denotes the quality of the solution it represents.
- **Population:** In order to look for the best solution, a group of individuals is managed. An initial population is created randomly, and will change across time, evolving towards members with different (and supposedly better) characteristics.
- **Breeding:** Several operators can be used to emu-
late the breeding process present in nature: mixing different individuals (crossover) or changing a particular one (mutation). These operators are used to obtain new individuals, expected to be better than the previous ones.

In the last two decades, Genetic Algorithms have been widely used to solve different problems, improving in many cases the results obtained by previous approaches. However, GAs require a large number of parameters (for example, those that control the creation of new individuals) that need to be correctly tuned in order to obtain good results. Generally, only experienced users can do this correctly and, moreover, the task of selecting the best choice of values for all these parameters has been suggested to constitute itself an optimization problem [11]. In addition, GAs show a poor performance in some problems (deceptive and separable problems) in which the existing crossover and mutation operators do not guarantee that better individuals will be obtained changing or combining existing ones.

Some authors [2] have pointed out that making use of the relations between genes can be useful to drive a more “intelligent” search through the solution space. This concept, together with the limitations of GAs, motivated the creation of a new type of algorithms grouped under the name of Estimation of Distribution Algorithms (EDAs).

EDAs were introduced in the field of Evolutionary Computation in [12], although similar approaches can be previously found in [13]. In EDAs there are neither crossover nor mutation operators. Instead, the new population of individuals is sampled from a probability distribution, which is estimated from a database that contains the selected individuals from the current generation. Thus, the interrelations between the different variables that represent the individuals are explicitly expressed through the joint probability distribution associated with the individuals selected at each generation. A common pseudo-code for all EDAs is presented in Fig. 2.

Steps 3, 4 and 5 will be repeated until a certain stop criterion is met (e.g., a maximum number of generations, a homogeneous population or no improvement after a specified number of generations). The probabilistic model learnt at step 4 has a significant influence on the behavior of the EDA from the point of view of complexity and performance.

For detailed information about the characteristics of EDAs, and the algorithms that form part of this family, see [14], [15], [16], [17].

IV. THE UMDAc ALGORITHM

The Univariate Marginal Distribution Algorithm for the continuous domain (UMDAc) [18], [19], is an EDA which supposes that there is not any dependency between the variables involved in the problem. It assumes that the joint density function follows a n-dimensional normal distribution, which is factorized by a product of one-dimensional and independent normal densities. In every generation and for every variable, the UMDAc performs some statistical tests in order to find the density function that best fits the sampling of that variable.

The UMDAc is a structure identification algorithm because the density components of the model to be learn are identified via hypothesis tests. This estimation of parameters is performed, after the densities are identified, by their maximum likelihood estimates. If all the univariate distributions are normal, then the two parameters to be estimated at each generation and for each variable are the mean, $\mu^i_l$, and the standard deviation, $\sigma^i_l$. It is well known that their respective maximum likelihood estimates are:

$$\hat{\mu}^i_l = \frac{1}{N} \sum_{r=1}^{N} x^i_{l,r}$$

$$\hat{\sigma}^i_l = \sqrt{\frac{1}{N} \sum_{r=1}^{N} (x^i_{l,r} - \hat{\mu}^i_l)^2}$$

V. PARALLELIZATION OF UMDAc

Evolutionary Algorithms require, in general, long execution times. For this reason, researchers often apply parallel techniques to reduce running times. These techniques are also useful to improve accuracy or to manage larger problems with the same time budget [20],[2].

There are two basic approaches to parallelize EAs: parallelization of program loops, and division of the population into several independent subpopulations (islands model). When using the islands approach, the single population used in sequential algorithms is split into several sub-populations (islands). These islands evolve independently, and exchange information about their best individuals with a predefined frequency. These models are suitable to distributed systems, because each island can be mapped onto a
separate processor, and the amount of communications required between islands is not very large. A more conservative approach starts with a sequential algorithm like that described in Figure 2, parallelizing parts of it in order to speed-up the execution time but without changing the semantics of the algorithm. There exist different proposals for GAs [21] or EDAs [22], [23], [24]. The most time-consuming portions of the code are identified and rewritten to take advantage of a parallel computer. Among the techniques to parallelize the code, or portions of it, the Manager-Worker model is a popular one: a Manager task runs the program, and delegates CPU-intensive parts to a collection of Worker tasks.

The selection of the parallelization paradigm has to be done taking into account the characteristics of the available computing platform. We will not work with a cluster of computers, but with on-chip multi-processors – in particular, with a Cell system. The limited memory of the Cell’s SPEs does not allow us to run a complete EDA (an island) in each SPE. Therefore, we have to opt for the Manager-Worker approach. The Manager task will run on the PPE and the Workers on the SPEs.

The parallel approach has been done starting from a sequential version of UMDA, written in C++. Before designing the parallel version for the Cell, we considered interesting, for comparison purposes, to design a parallel version based on the Posix Threads (pthreads) library [25], that could be executed on a multi-core personal computer. Also, as both multi-core Intel-based machines and the Cell include vector instructions (that can accelerate our application), we have also evaluated manually vectorized versions of the code.

Following the Manager-Worker scheme, the UMDA algorithm will be executed by the main thread (Manager), and when necessary, it will ask the Workers for help. In particular, workers will collaborate in these phases:

- Learning the probabilistic model: As introduced previously, UMDA uses a very simple probabilistic model, that assumes that there is no relation between the variables. Therefore, once the population has been selected, the Manager will ask the workers to obtain parts of the mean and standard deviation –our implementation assumes normal distributions, for a subset of the selected population. Once each Worker has finished, the Manager creates the main model based on the partial values.

- Sampling and Evaluation: These two steps usually come together. That is, based on the model learnt in the previous step, new individuals will be created and evaluated. Again, the Manager will ask the workers to create (and evaluate) a subset of individuals. The number of individuals to be managed by each worker can be established statically, or assigned dynamically using an on-demand scheme. That is, when the evaluation of the individuals takes always the same computing time, a static assignation can be done. However, if the time required to evaluate the individual depends on the values it takes, the on-demand scheme would be preferable.

In order to test the performance of our different implementations of UMDA, we used them to solve an artificial problem, the Griewangk minimization problem [26]. The fitness function is defined as follows:

\[
F(x) = 1 + \sum_{i=1}^{n} \frac{x_i^2}{4000} - \prod_{i=1}^{n} \cos \left( \frac{x_i}{\sqrt{i}} \right)
\]  

The range of all the variables of the individual is \(-600 \leq x_i \leq 600, i = 1, \ldots, n\), and the fittest individual corresponds to a value of 0, that only can be obtained when all the variables of the individual are 0.

VI. MEASURING THE PERFORMANCE OF THE UMDA

In order to test the performance of this multi-threaded version, we completed several experiments on an Intel Xeon Quad-Core computer. Different individual sizes were used (ranging from 100 to 3,000 variables), using a population size of 2,5L, being L the number of variables of the individual. Tests were performed with 1-4 threads. UMDA was stopped after computing 50 generations. The results of these experiments are shown in Figure 3.

According to the results, it can be seen that the multi-threaded version has an adequate behavior from the point of view of scalability. Therefore, the second step of this work would be to test the suitability of the Cell for the execution of this EDA.

We have made the same experiment with the Cell version executed over a PS3. In this case, individual sizes range from 100 to 1,800 variables (due to limitations on the SPE’s local store). The number of threads (running in different SPEs) was varied from 1 to 6. The rest of the parameters – population size, stopping criterion – were as in the previous experiments. Results can be seen in Figure 4. Clearly, the solution scales with the number of SPEs, providing...
good performance levels. This is good news because, as reported in our previous work [6], for the UMDA applied to discrete domains, the performance of Cell was very poor. Therefore, we can state that the Cell is a more suitable platform to run UMDA, (continuous domain, floating-point numbers).

Vector processors give us the possibility to operate over multiple data with a single machine instruction. As the two platforms used in our experiments integrate support for vector operations, we decided to modify the UMDA implementations to take advantage of this feature. One of the more expensive parts of the UMDA is the sampling and evaluation of new individuals. In the sampling step, an adaptation of the Probabilistic Logic Sampling (PLS) for the continuous domain is used. This technique needs random values to create new individuals, and thanks to the vectorization, the process of obtaining these random values can be done in groups of four. A similar idea was applied to the evaluation of the individuals, rewriting the evaluation function to compute the different operations: square root, cosine, square, etc. in groups of four.

The vectorized version of the Cell implementation was made using SPU intrinsics [27] and the libmisc library included in the IBM Cell SDK [28], which implements vectorized versions of a uniform random number generator. For the Intel platform, we used SSE intrinsics [29] and implemented our own vectorized version of a linear congruential generator [30].

We repeated the experiments with the vectorized implementations of UMDA. Results are shown in Figures 5 and 6. Note that the scale (X axis) for each figure is different. As we can observe, the acceleration levels obtained via vectorization are impressive for both platforms. In Figure 7 we have plotted the scalar/vector acceleration ratio (speedup) for 1 thread (Xeon) and 1 SPU (Cell) for different individual sizes. We can see that for the Xeon platform the maximum speedup is achieved for individuals of size larger than 300, and that this figure remains stable for longer individuals. However, for the Cell, a peak is observed for individuals of size 500, but for larger problems speedup drops. We need to further explore this issue, but we suspect that the cause is on the bottlenecks in the internal Cell interconnection network, which saturates when large DMA transfers occur too often – that is, when the application is too communication-biased.

When comparing the two platforms, Figure 3 versus Figure 5, and Figure 4 versus Figure 6, we can observe that, even using vectorized code, the Xeon Quad-Core is one magnitude order faster. In the selection of the best platform we can not forget the cost of each solution. In terms of code development, the Xeon Quad-Core is an easier platform to program multi-thread code but harder at the vectorization process than the Cell. Also if we compare their prices, the cheapest Cell platform, the PlayStation 3, is about half price the Xeon Quad-Core, giving us an enormous computing power for a budget.

VII. Conclusions

In this paper we have evaluated several parallel implementations of UMDA, on two different platforms: a Quad-Core Intel Xeon and a Cell (PlayStation 3) system. We have shown that the well-known Manager-Worker parallelization scheme can be successfully applied to port our algorithm to these platforms: in both cases we are capable of exploiting the availability of multiple cores, homogeneous for the Xeon system, and heterogeneous for the Cell. Additionally, as all the processors involved in our
The programs perform exceedingly well, providing additional speedups on the 5-9 range (depending on the platform and the problem size).

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Fig. 7. Impact of vectorization in the Xeon Quad-Core and the Cell.

The experiments integrate support for vector operations, we have tested manually vectorized versions of the programs, which were implemented using different repertoires of intrinsics. The vectorized versions of the programs perform exceedingly well, providing additional speedups on the 5-9 range (depending on the platform and the problem size).